



## Theoretical Enhancement of Point Resistance in Sandy Soils Using Bio-Inspired Cranial Asperity Ratios

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### Abstract

This study aims to enhance the bearing capacity of pile foundations in sandy soils through a bio-inspired approach by modifying Meyerhof's empirical equation using a cranial correction factor. The adjustment considers the geometric influence of the asperity length–height ratio ( $L/H$  20, 26.67, and 33.33) applied to different pile diameters. The analysis was carried out theoretically by calculating point resistance ( $Q_p$ ) using the modified equation, followed by validation through ANOVA and the nonparametric Mann–Whitney test. The results indicate that an  $L/H$  ratio of 20 provides the most significant improvement in  $Q_p$ , ranging from 11.7% to 465.8% compared to the conventional Meyerhof model, particularly at lower  $D/B$  ratios where stress concentration can be optimally mobilized. Larger ratios such as 26.67 and 33.33 also improve capacity, though less effectively than  $L/H$  20, yet still outperform unmodified foundations. The correction factors obtained, ranging from  $C_r$  1.07 to 5.66, demonstrate the substantial contribution of geometric modification to load transfer efficiency. The novelty of this research lies in integrating anisotropic interface properties into the classical Meyerhof model, thereby bridging the gap between isotropic predictions and anisotropic experimental evidence. Accordingly, the developed theoretical framework not only strengthens the basis for calculating pile bearing capacity but also opens new avenues for bio-inspired foundation design that is more efficient and sustainable.

**Keywords:** Cranial Foundation;  $L/H$  Ratio; Modified Meyerhof Equation; Point Resistance; Load Transfer Efficiency.

### 1. Introduction

The optimization of pile foundation bearing capacity in sandy soils remains a pivotal challenge in contemporary geotechnical engineering [1, 2], owing to its critical role in ensuring structural stability and resource efficiency [3]. Classical empirical models, such as that proposed by Meyerhof, are extensively employed due to their simplicity; however, they inherently assume isotropic conditions at the soil–structure interface [4]. Consequently, the predicted tip and shaft resistances frequently underestimate the capacities observed in experimental investigations [5]. This discrepancy underscores the necessity for innovative approaches capable of more realistically capturing the mechanisms of soil–structure interaction, particularly by accounting for surface geometry, directional shear effects, and cyclic response under repeated loading, which are prevalent in practical foundation applications [6].

The phenomenon of anisotropic friction in snakes [7] has long attracted attention in biomechanics and tribology studies [8]. Snake locomotion exhibits a significant difference between cranial and caudal directions, with higher frictional resistance occurring during forward (cranial) movement [1]. Direct shear tests on ventral scales have demonstrated that cranial orientation can mobilize peak resistance up to 6.0 kPa and residual resistance of 9.1 kPa, whereas unidirectional cranial testing recorded an increase up to 22.0 kPa at a contact area of 0.21 [9]. This mechanism

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arises from the asymmetry of microstructural scales and serves as the fundamental inspiration for designing more efficient foundations through mechanical interlocking with soil grains [10, 11].

The application of directionally textured surfaces at the soil–structure interface has been proven to enhance load transfer [12]. Experimental studies have reported that bio-inspired piles can achieve a shaft friction ratio ranging from 2.98 to 16.36 in the cranial direction, substantially higher than that of rough steel piles, which is only about 4.0 [12]. Although this improvement is significant, technical drawbacks such as increased driving resistance and potential asperity wear remain as challenges for practical implementation [6]. In this context, load transfer efficiency is defined as the ability of foundations to transmit loads with minimal energy loss at the interface [10, 11]. Normalized roughness ratio ( $R_n$ ) and asperity length-to-height ratio ( $L/H$ ) serve as key parameters. Laboratory tests have shown that increasing  $R_n$  from 0.01 to 0.06 can raise the  $\delta_{cs}/\phi_{cs}$  ratio from 0.7 to 1.2, illustrating how minor changes in asperity geometry can yield considerable frictional gains [13]. Biomimetic studies based on the scales of *Leptophis ahaetulla* have identified an  $L/H$  ratio of approximately 20–33 as optimal for maximizing frictional anisotropy [14, 15].

Further experimental evidence substantiates this phenomenon, as a 10 mm pile with  $L/H$  40 in Ottawa F65 sand was reported to exhibit a 780% increase in uplift capacity compared to a smooth pile [6]. At  $L/H$  20, shaft capacity reached 6.3 MN at a depth of 11.6 m, representing an 845% improvement over the smooth pile [16]. Discrete Element Method (DEM) simulations with a 40 mm pile and  $L/H$  18.75 demonstrated a 154% increase in axial capacity under cranial installation compared to caudal installation [17]. These findings confirm that asperities with smaller  $L/H$  ratios generate stronger soil interlocking, albeit with the consequence of higher installation resistance [18]. Moreover, cyclic loading studies revealed that anisotropically textured foundations are more capable of maintaining load-bearing capacity after multiple loading cycles, whereas smooth piles tend to degrade due to interface frictional loss. The cyclic tests indicated that cranial-oriented piles exhibited greater resistance. In dense sand at  $L/H$  20, cranial capacity decreased from 0.90 to 0.37, while caudal capacity dropped from 0.42 to 0.18. At  $L/H$  40, cranial piles still retained approximately 43% of their initial capacity [6].

The bearing capacity of pile foundations originates from the plastic behavior of materials under load, as described by Prandtl [19], and the application of differential equations by Reissner [20]. The ultimate soil bearing capacity ( $Q_u$ ) is expressed as the sum of the pile's point resistance ( $Q_p$ ) and skin resistance ( $Q_s$ ) [21–23]. Key factors influencing this capacity include the pile size ( $A$ ) [24], the depth of the loaded area ( $D$ ), and the bearing capacity factor ( $N_q$ ), which depends on the soil's internal friction angle. For various friction angles,  $N_q$  values range from 1 to 81.27 ( $0^\circ$  -  $40^\circ$ ) [25], 1 - 392.8 ( $0^\circ$  -  $50^\circ$ ), and 12.4 - 930 ( $20^\circ$  -  $45^\circ$ ) [4]. In the case of skin resistance ( $Q_s$ ), the correction factor ( $K$ ) adjusts for vertical soil stress [26, 27]. This factor was initially introduced by Meyerhof [28] and later refined by  $K$  researchers such as [28–30]. The soil's friction angle influencing typically falls within  $33^\circ$  to  $43^\circ$  [31], with specific studies reporting values as high as  $38.5^\circ$  [32–34].

Although these studies highlight the significant potential of bio-inspired approaches, classical empirical models such as Meyerhof [4] still assume isotropic conditions. As a result, the predicted point resistance ( $Q_p$ ) tend to be lower than the outcomes observed in anisotropic experimental studies. This research gap remains unaddressed, as no analytical modification of Meyerhof's equation has yet incorporated anisotropy factors into the calculation of point resistance.

This study proposes a modification of Meyerhof's equation by introducing a Cranial Correction Factor ( $C_r$ ), which represents the contribution of anisotropic friction from cranial asperities. The analysis was conducted on piles with diameters of 10 mm, 12 mm, and 15.85 mm, with  $L/H$  ratios of 20, 26.67, and 33.33. These ratios were selected as they correspond to the concave scale morphology of *Leptophis ahaetulla*, which has been shown to be the most efficient in generating frictional anisotropy. Theoretical validation was carried out using Analysis of Variance (ANOVA) to evaluate the significance of this parameter's influence on  $Q_p$  at a 95% confidence level. The use of ANOVA is considered appropriate as an initial validation step prior to subsequent laboratory testing and numerical simulations.

The main contribution of this study lies in introducing a new dimension to the calculation of foundation bearing capacity by integrating anisotropic interface properties into the classical Meyerhof model. In doing so, the study bridges the gap between conventional isotropic models and anisotropic empirical evidence, while providing a theoretical framework with potential applications in the design of bio-inspired textured foundations. Accordingly, this research not only establishes a novel theoretical framework but also lays the groundwork for future experimental validation, making its outcomes relevant both academically and practically for bio-inspired foundation design.

The overall structure of this article is illustrated in Figure 1. It begins by introducing the background, motivation, and objectives that frame the research problem. This is followed by a presentation of the theoretical framework and the modified equations adopted to describe the load transfer mechanisms, which form the analytical foundation of the study. The paper then outlines the parametric configurations employed in the analysis, including variations in interface anisotropy and geometric ratios. Subsequently, the results derived from the theoretical models are discussed and interpreted in light of existing knowledge. Finally, the paper concludes by summarizing the main findings, highlighting limitations, and providing recommendations for future experimental validation.

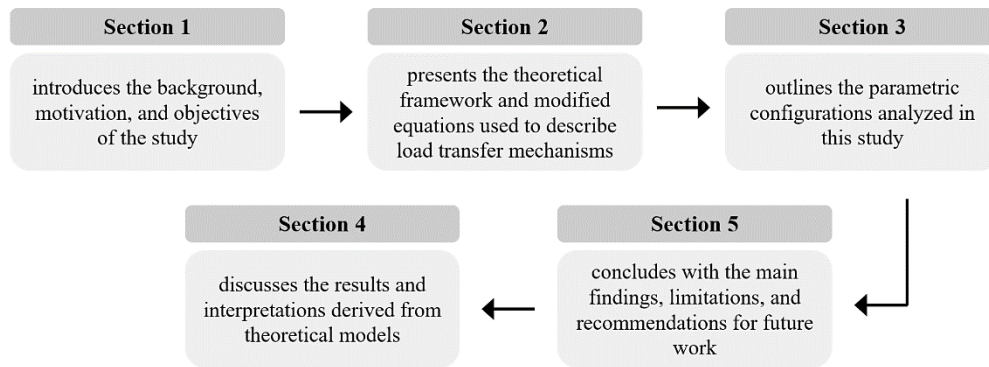


Figure 1. Structure Of This Article

## 2. Materials and Methods

The stages of this research are presented in Figure 2, where this study is entirely theoretical, building on Figure 3, which illustrates the geometric influence of the  $L/H$  ratio derived from cranial-inspired mechanisms. Using this basis, Meyerhof's empirical equation is modified to evaluate point resistance ( $Q_p$ ) by incorporating soil properties such as friction angle ( $\phi$ ), and dry density ( $\gamma_t$ ). The modification emphasizes the improvement in load transfer efficiency, demonstrating the critical role of asperity geometry in enhancing soil-structure interaction.

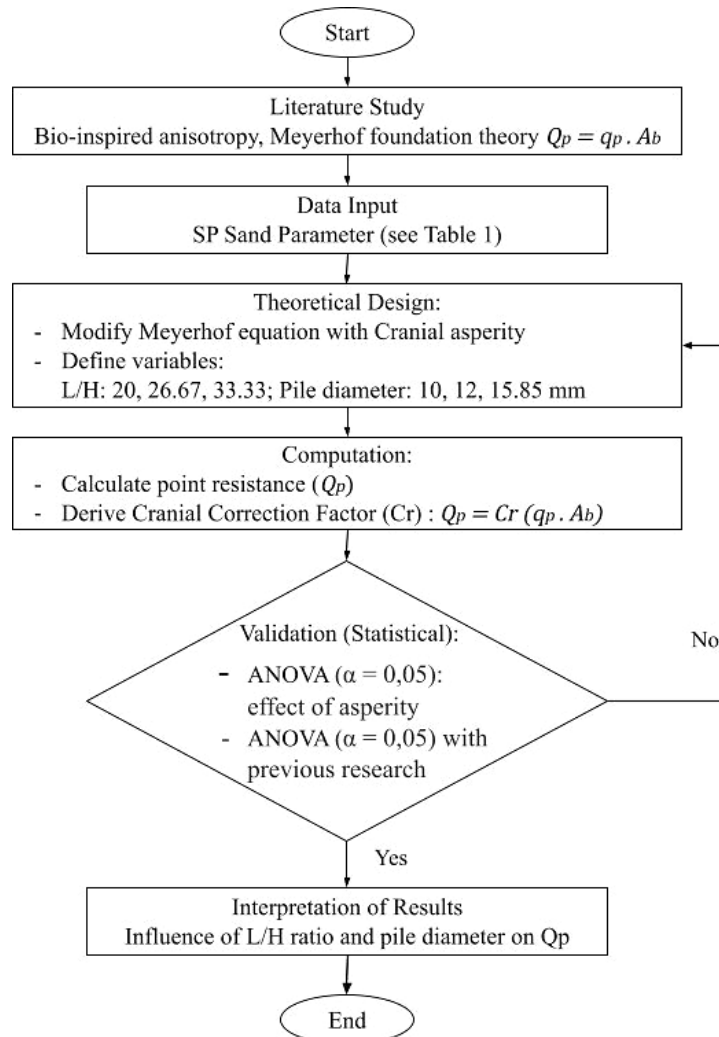
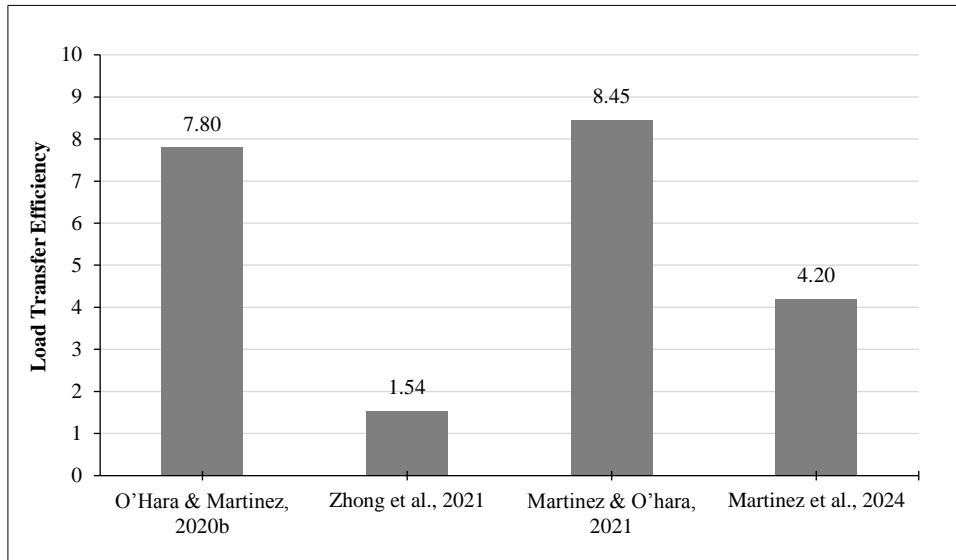


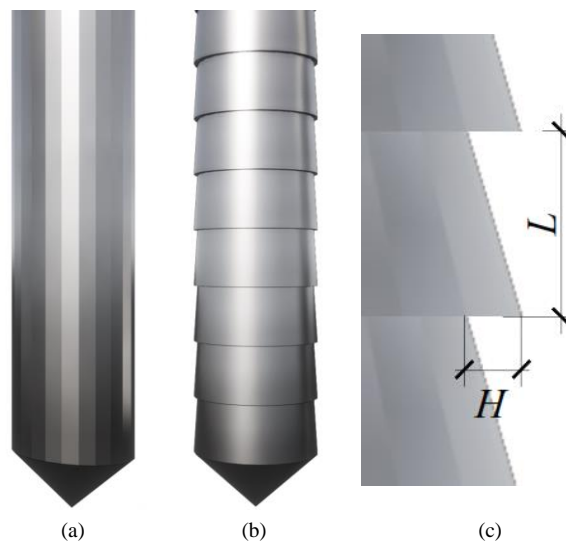
Figure 2. Flowchart of the Research

Three  $L/H$  ratios (20, 26.67, and 33.33) were prescribed to represent steep, moderate, and gentle asperity inclinations. The asperity height ( $H$ ) was kept constant across configurations, while the asperity length ( $L$ ) was varied to change  $L/H$ , enabling an isolated assessment of its effect on point resistance ( $Q_p$ ). Figure 4 presents the schematic

representation of the piles used as the basis for theoretical calculations. Table 1 summarizes the soil properties applied in these calculations, which were incorporated into a modified equation to determine  $Q_p$ , values across different configurations.



**Figure 3. Basic Previous Research**



**Figure 4. (a) Reference Foundation, (b) Cranial Foundation, (c)  $L/H$  Details**

**Table 1. Sand Properties**

Properties	Value
Sand Type	SP
Dr (%)	70
Dry unit weight ( $\gamma_t$ ) [kN/m <sup>3</sup> ]	16.69
Uniformity coefficient Cu	3.42
Coefficient of curvature Cc	0.96
Average particle size $D_{50}$ [mm]	0.40
Void ratio (e)	0.71
Maximum void ratio $e_{max}$	0.91
Minimum void ratio $e_{min}$	0.62
Porosity (%)	38.24
Specific Gravity ( $G_s$ )	2.76
Friction angle $\phi$ [°]	30

No load tests or numerical simulations using software were conducted. The results are derived solely from the theoretical application of the modified Meyerhof equation, ensuring a focus on mathematical relationships between soil properties, pile geometry, and the  $L/H$  ratio. In the context of foundation-point resistance [4], developed the point resistance equation ( $Q_p$ ), which is generally expressed as follows:

$$Q_p = q_p \cdot A_b \quad (1)$$

$$Q_p = \sigma' \cdot N_q \cdot A_b \quad (2)$$

where, point resistance ( $Q_p$ ), bearing capacity of pile point ( $q_p$ ), point surface area ( $A_b$ ), Meyerhof bearing capacity factor ( $N_q$ ), overburden effective stress ( $\sigma'$ ).

Statistical validation of the theoretical calculations was conducted using Analysis of Variance (ANOVA). ANOVA was selected as it conforms to the data assumptions and effectively compares means across groups. However, non-parametric tests such as the Mann–Whitney test or sensitivity analysis can also be employed as complementary approaches to provide additional confidence in the results [35-37]. In this study, ANOVA was employed to assess the impact of the  $L/H$  ratio and pile diameter on the point resistance ( $Q_p$ ). The F-statistic and p-values were computed to evaluate the significance of these parameters, with a significance level ( $\alpha$ ) set at 0.05. The analysis revealed statistically significant differences among the tested configurations, highlighting the critical role of geometric modifications in improving point resistance ( $Q_p$ ) [38].

### 3. Results and Discussion

#### 3.1. Results

Based on Figure 5, the inclusion of  $q_{pcr}$  in the  $L/H$  profile of cranial foundations necessitates modifications to Meyerhof's original equations (Equations 1 and 2). These adjustments result in equations (Equations 3 and 4), which refine the calculated  $Q_p$  values. The presence of  $q_{pcr}$  along the shaft of the pile significantly influences the overall  $Q_p$ , as it alters the distribution of forces along the pile surface. Consequently, a correction factor is introduced to account for the  $L/H$  ratio specific to cranial foundations, modifying Meyerhof's equation for  $Q_p$ . The resulting equation, integrating the cranial correction, is derived as follows:

$$Q_{pcr} = Q_p + (q_{pcr} \cdot A_{bcr} \cdot N_{sb}) \quad (3)$$

$$Q_{pcr} = (q_p \cdot A_b) + (q_{pcr} \cdot A_{bcr} \cdot N_{sb}) \quad (4)$$

$$Q_{pcr} = (\sigma' \cdot N_q \cdot A_b) + (\sigma' \cdot N_q \cdot A_{bcr} \cdot N_{sb}) \quad (5)$$

$$Q_{pcr} = \left( \sigma' \cdot N_q \cdot \left( \frac{1}{4} \pi \cdot B^2 \right) \right) + \left( \sigma' \cdot N_q \cdot \left( \left( \frac{1}{4} \pi \cdot B^2 \right) - \left( \frac{1}{4} \pi \cdot B_{cr}^2 \right) \right) \cdot N_{sb} \right) \quad (6)$$

$$C_r = \frac{(\sigma' \cdot N_q \cdot \left( \left( \frac{1}{4} \pi \cdot B^2 \right) - \left( \frac{1}{4} \pi \cdot B_{cr}^2 \right) \right) \cdot N_{sb})}{(\sigma' \cdot N_q \cdot \left( \frac{1}{4} \pi \cdot B^2 \right))} \quad (7)$$

$$C_r = \frac{Q_{pcr}}{Q_p} \quad (8)$$

The following terms are defined for the analysis: point resistance ( $Q_p$ ), and cranial point resistance ( $Q_{pcr}$ ), refer to the point load resistance at the pile tip, with cranial variations incorporating asperities at the pile interface. The point bearing capacity of the pile tip ( $q_p$ ), and its cranial counterpart ( $q_{pcr}$ ), represent the stress distribution at the pile point. Point surface area ( $A_b$ ), and cranial point surface area ( $A_{bcr}$ ), are calculated based on the pile geometry. Other parameters include pile diameter ( $B$ ), Meyerhof bearing capacity factor ( $N_q$ ), overburden effective stress ( $\sigma'$ ), point total asperities ( $N_{sb}$ ), and cranial point resistance asperities factor ( $C_r$ ) which modifies the point resistance for cranial profiles.

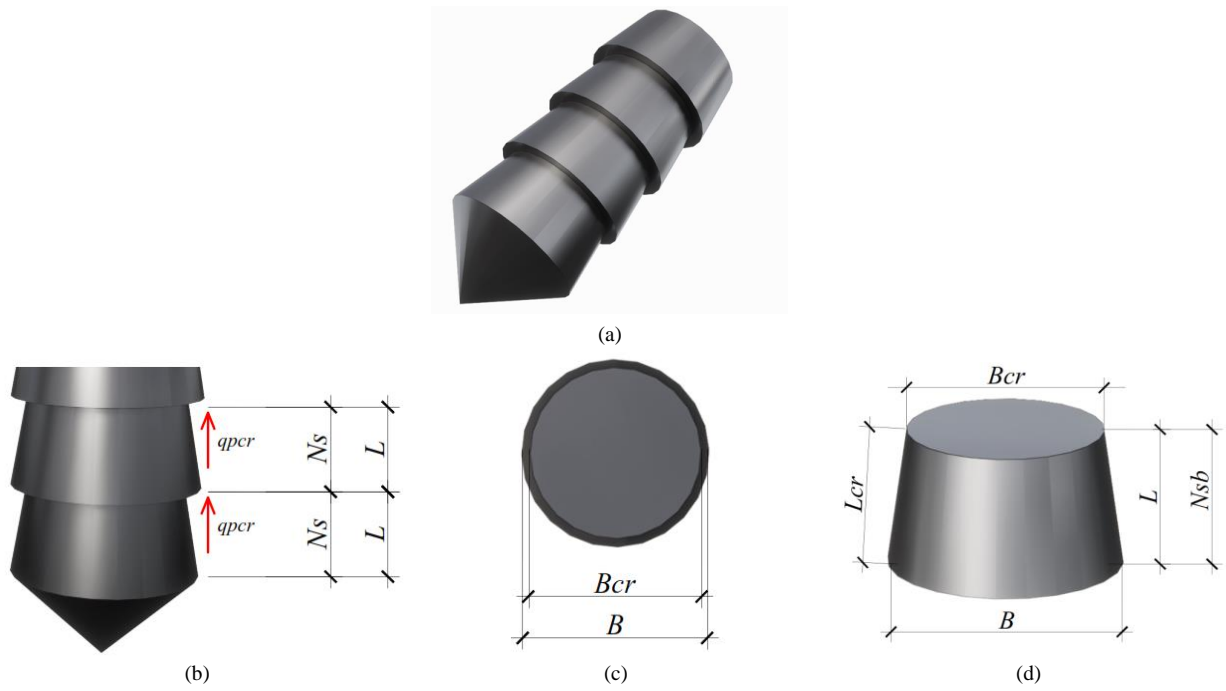


Figure 5. (a) 3D Detail of Cranial Foundations (b) Front View Detail of Cranial Foundations (c) Top View Detail of Cranial Foundations (d) Cross-section Detail of Cranial Foundations

### 3.1.1. Depth ( $D$ ) vs Point Resistance ( $Q_p$ )

In Figure 6, all combinations of pile diameter ( $B = 10, 12, 15.85$  mm) and asperity ratios ( $L/H = 20, 26.67, 33.33$ ) demonstrate an increase in point resistance  $Q_p$  with increasing depth  $D$  in the range of 10–240 mm.

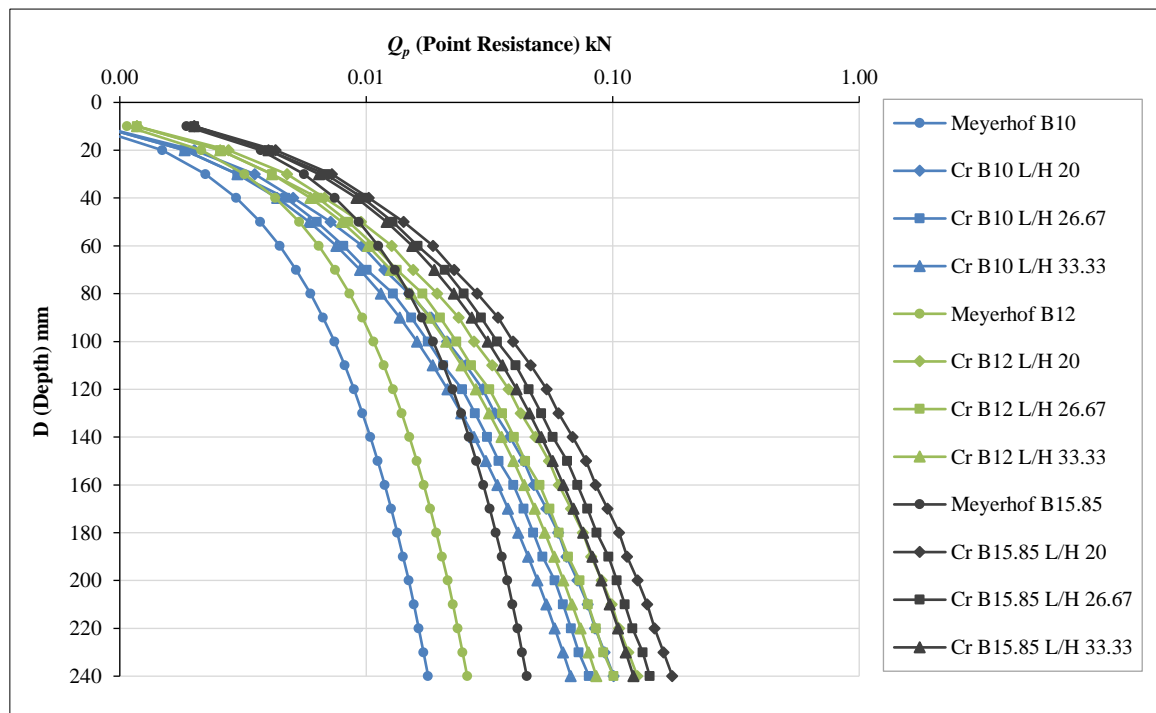


Figure 6. The Graph of the Depth ( $D$ ) vs Point Resistance ( $Q_p$ )

In Figure 7, at a depth of  $D = 80$  mm, the Meyerhof model with  $B = 15.85$  mm produced  $Q_p = 0.015$  kN; The cranial curve with  $B = 10$  mm and  $L/H = 20$  ( $L = 6$ ) reached the same  $Q_p$  value, despite having a smaller diameter, with a difference of 5.85 mm or 36.9% relative to  $B = 15.85$  mm. This finding indicates that cranial texturing can partially compensate for the reduced cross-sectional area of smaller piles by enhancing interface resistance. Consequently, pile geometry optimization through surface anisotropy may be as critical as increasing pile diameter in improving point resistance.

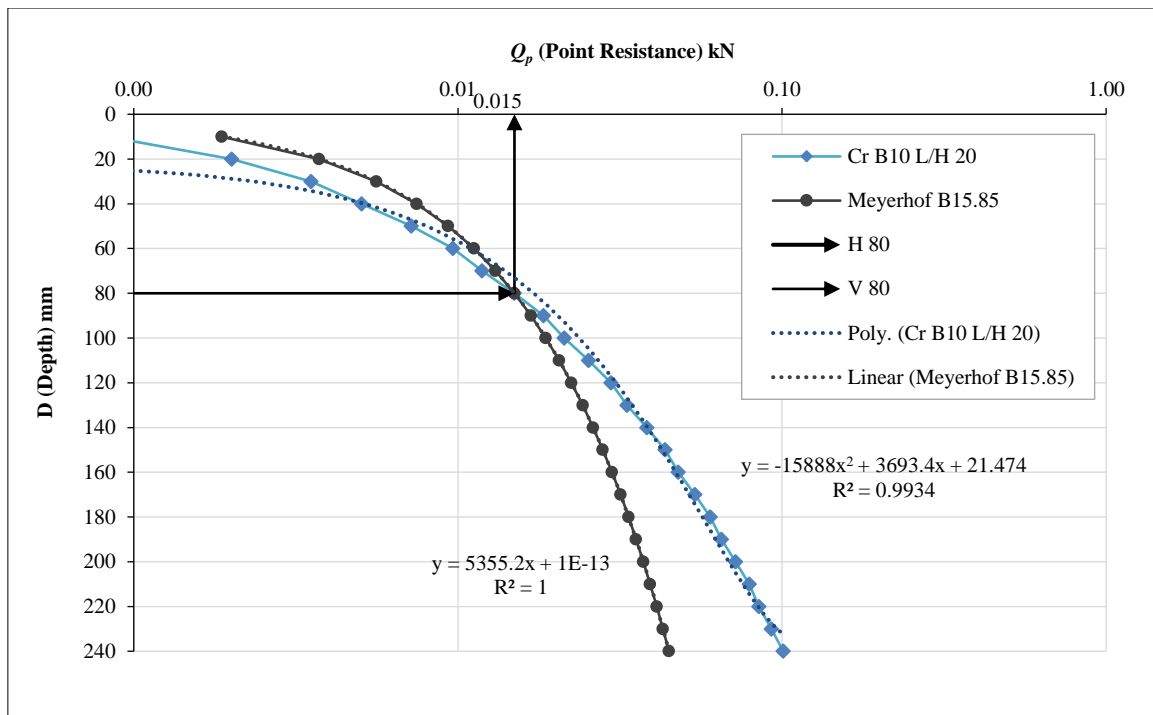


Figure 7. The Graph of the Relationship between Cranial B10 and Meyerhof B15.85

### 3.1.2. Depth/Diameter Ratio ( $D/B$ ) vs Point Resistance ( $Q_p$ )

In Figure 8,  $Q_p$  is plotted against the depth–diameter ratio ( $D/B = 2\text{--}24$ ) for all pile diameter combinations  $B$  (10, 12, 15.85 mm) and asperity ratios  $L/H$  (20, 26.67, 33.33). Figure 9 illustrates two intersection points yielding the same  $Q_p$  values at  $D/B = 6$  between the Meyerhof model for  $B = 15.85$  mm and the cranial configuration of  $B = 10$  mm with  $L/H = 20$ ; and at  $D/B = 14$  between the Meyerhof model for  $B = 15.85$  mm and  $B = 12$  mm,  $L/H = 20$ . The regression equations obtained ( $x = D/B$  and  $y = Q_p$  in kN) are as follows: Meyerhof  $B = 15.85$  mm,  $y = -625.77x^2 + 224.72x + 1.9447$  ( $R^2 = 0.9936$ ), cranial  $B = 12$  mm,  $L/H = 20$ ,  $y = -1185.2x^2 + 336.85x + 2.4786$  ( $R^2 = 0.9928$ ), and cranial  $B = 10$  mm,  $L/H = 20$ ,  $y = 337.86x + 6 \times 10^{-15}$ .

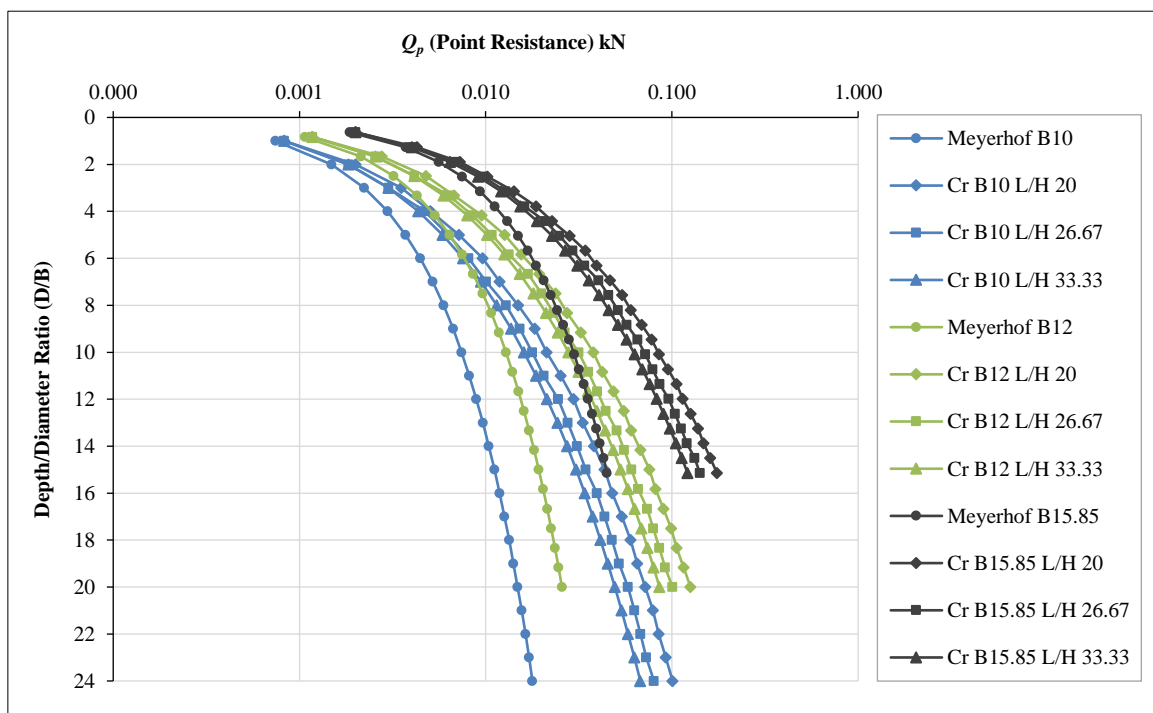


Figure 8. The Graph of the Relationship between Depth/Diameter Ratio ( $D/B$ ) vs Point Resistance ( $Q_p$ )



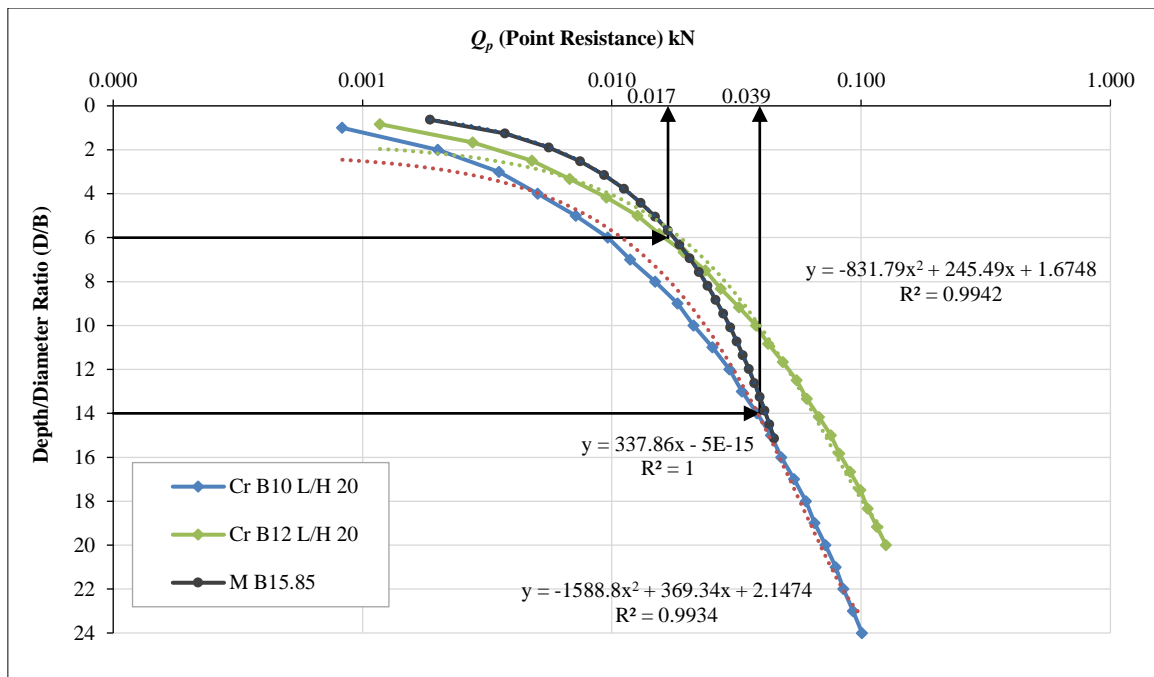


Figure 9. The Graph of the Relationship between Cranial B10 and Meyerhof B15

### 3.1.3. Depth/Diameter ( $D/B$ ) vs Increase in Point Resistance ( $\Delta Q_p$ )

In Figure 10, the increase in point resistance ( $\Delta Q_p$ ) is defined as  $Q_{pcr} - Q_p$  and is plotted against the  $D/B$  ratio for all cranial configurations. At  $D/B = 14$ , the configuration with  $B = 10$  mm and  $L/H = 20$  yielded the lowest  $\Delta Q_p$  value among the curves presented. At the same ratio, the curves for  $B = 10$  mm,  $L/H = 20$  and  $B = 12$  mm,  $L/H = 26.67$  were nearly coincident. The  $\Delta Q_p$  (kN) axis scale in the graph was set at 0.005, 0.010, and 0.028.

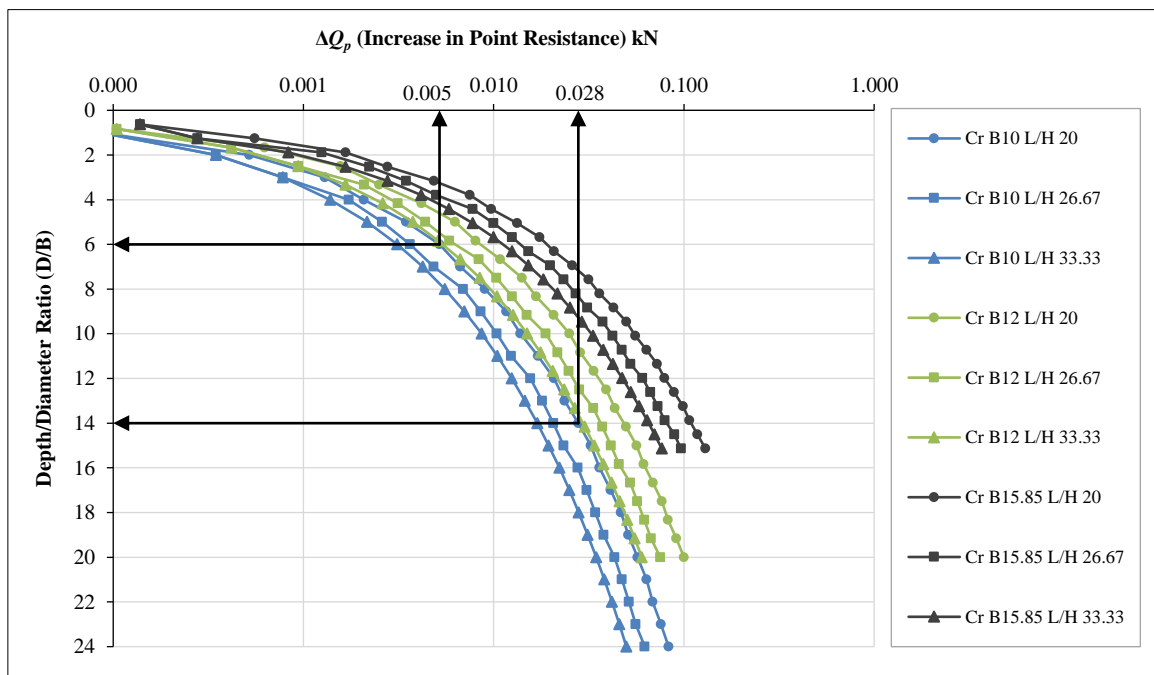


Figure 10. Graph Relationship between Depth/Diameter Ratio ( $D/B$ ) vs Increase in Point Resistance ( $\Delta Q_p$ )

### 3.1.4. Range of $Q_p$ Enhancement Relative to Meyerhof

The range of  $Q_p$  enhancement (in percentage) relative to Meyerhof's predictions, as referenced from Figures 4 to 6 at depths of  $D = 10$ – $240$  mm, is summarized as follows. For  $L/H = 20$ , the configurations with  $B = 10$ ,  $12$ , and  $15.85$  mm exhibited increases of  $11.7$ – $465.8\%$ ,  $9.7$ – $390.0\%$ , and  $7.4$ – $289.7\%$ , respectively. At  $L/H = 26.67$ , the corresponding ranges were  $11.7$ – $349.4\%$ ,  $9.7$ – $292.5\%$ , and  $7.4$ – $215.4\%$  for  $B = 10$ ,  $12$ , and  $15.85$  mm. At  $L/H = 33.33$ , the values recorded were  $11.7$ – $279.5\%$ ,  $9.7$ – $234.0\%$ , and  $7.4$ – $170.8\%$  for the same diameters.



### 3.1.5. Meyerhof Equation Correlation

The theoretical results indicate that Meyerhof's equation for calculating the point resistance ( $Q_p$ ) requires adjustments to account for the influence of the  $L/H$  ratio on cranial foundations. Based on the theoretical analysis presented in Table 1, the required modifications for each  $L/H$  ratio are as follows:

- $L/H$  20

$$Q_p = (1.07 - 5.66) q_p \cdot A_b \quad (9)$$

At this ratio, the increase in  $Q_p$  ranges from 11.7% to 456.8% range for  $B10$ , 9.7% to 390% range for  $B12$ , and 7.4% to 289.7% range for  $B15.85$  compared to the Meyerhof foundation at depths between 10 to 240 mm.

- $L/H$  26.67

$$Q_p = (1.07 - 4.49) q_p \cdot A_b \quad (10)$$

For this ratio, the increase in  $Q_p$  ranges from 11.7% to 349.4% for  $B10$ , 9.7% to 292.5% range for  $B12$ , and 7.4% to 215.4% for  $B15.85$  at depths between 10 to 240 mm. This indicates that the stress distribution and soil-pile interaction remain efficient, though slightly less optimal compared to  $L/H$  20.

- $L/H$  33.33

$$Q_p = (1.07 - 3.79) q_p \cdot A_b \quad (11)$$

At this ratio, the cap  $Q_p$  increase s only around 11.7% to 279.5% range for  $B10$ , 9.7% to 234.0% for  $B12$ , and 7.4% to 170.8% for  $B15.85$  at depths between 10 to 240 mm.

### 3.1.6. Efficiency of Cranial Foundation Geometry

Cranial foundations with  $L/H$  20 achieve a  $Q_p$  equivalent to Meyerhof foundations but with a diameter reduction of up to 58.5%. The cranial point resistance asperities factor ( $C_r$ ), calculated as  $Q_{p_{cr}}/Q_p$ , quantifies the efficiency of capacity improvement due to asperity modifications. For diameters of 10, 12, and 15.85 mm,  $C_r$  values range from 1.07 to 5.66, indicating that higher values correspond to greater efficiency in enhancing bearing capacity

### 3.1.7. Statistical Validation

The ANOVA validation results in Table 2 confirm a statistically significant relationship between  $Q_p$  and  $Q_{p_{cr}}$  at a significance level of  $\alpha = 0.05$ . The F-Statistic values show variations among parameters  $B10$ ,  $B12$ , and  $B15.85$  across different  $L/H$  ratios. For instance, the highest F-Statistic value 20.27 is observed for  $B10$  with  $L/H$  20, while the lowest value 10.87 occurs for  $B15.85$  with  $L/H = 33.33$ . Additionally, all P-Values in the table are smaller than  $\alpha = 0.05$ . For example, for  $B10$  with  $L/H = 20$  has a P-Value is  $4.58 \times 10^{-5}$ , while  $B15.85$  with  $L/H = 33.33$  has a P-Value is  $1.89 \times 10^{-3}$ . These findings confirm that the relationship between  $Q_p$  and  $q_{p_{cr}}$  is significant at a 95% confidence level. The decreasing F-Statistic values with increasing  $L/H$  suggest that the  $L/H$  ratio influences the strength of this relationship.

Table 2. Validation of ANOVA  $Q_p$  with  $Q_{p_{cr}}$

Parameters	B10 (L/H)			B12 (L/H)			B15.85 (L/H)		
	20	26.67	33.33	20	26.67	33.33	20	26.67	33.33
F-statistic	20.27	17.80	16.14	18.85	16.21	14.43	15.79	13.03	10.87
P-Value	$4.58 \times 10^{-5}$	$1.14 \times 10^{-4}$	$2.16 \times 10^{-4}$	$7.69 \times 10^{-5}$	$2.10 \times 10^{-4}$	$4.25 \times 10^{-4}$	$2.47 \times 10^{-4}$	$7.53 \times 10^{-4}$	$1.89 \times 10^{-3}$

### 3.1.8. Comparison with Previous Studies

The Statistical analysis, referring to Table 3, was conducted to compare the  $C_r$  values from theoretical calculations (for diameters of 15.85 mm, 12 mm, and 10 mm) with data from studies [16, 39-42]. The data from these previous studies were extracted from Figure 3 for consistency and accuracy in comparison. The ANOVA test in Table 3 shows an F-statistic value of 2.305 with a P-value of 0.167 ( $P > 0.05$ ). Nonparametric validation using the Mann-Whitney test yielded a P-value of 0.166 ( $P > 0.05$ ). The consistency of these two methods confirms that there are no significant differences between the theoretical results and the previous study data.

**Table 3. Statistical Analysis of  $C_r$  Previous Research and This Research**

ANOVA (One-Way)		Nonparametric (Mann-Whitney)
F	P-value	P-value
2.305	0.167	0.166

The theoretical model used in this study has proven capable of accurately representing load transfer efficiency across various pile diameters and asperity configurations. Although some maximum values reported in studies [6, 12, 40] are slightly higher, the theoretical results remain within a relevant range. Therefore, as supported by the analysis in Table 3 and the data in Figure 1, this theoretical approach is valid for describing the load transfer mechanism in pile foundations.

### 3.2. Discussion

#### 3.2.1. $Q_p$ and $\Delta Q_p$ in Relation to $D$ and $D/B$

In Figure 6, the point resistance ( $Q_p$ ) increases with depth ( $D$ ) across all combinations of pile diameter ( $B$ ) and asperity ratio ( $L/H$ ). At  $D = 80$  mm, the  $Q_p$  value predicted by the Meyerhof model for  $B = 15.85$  mm coincides with that of the cranial configuration  $B = 10$  mm,  $L/H = 20$  (Figure 7). In the non-dimensional domain, the  $Q_p$  versus  $D/B$  plot exhibits the highest values at  $D/B \leq 24$ , whereas for  $D/B \geq 30$  the rate of increase becomes less pronounced (Figure 8). Curve intersections at  $D/B = 6$  and 14 illustrate configuration pairs producing identical  $Q_p$  values (Figure 7). The  $\Delta Q_p = Q_{p_{cr}} - Q_p$  plotted against  $D/B$  reveals the convergence of responses among certain cranial configurations; for example, at  $D/B = 14$ , the curve for  $B = 10$  mm,  $L/H = 20$  nearly coincides with that of  $B = 12$  mm,  $L/H = 26.67$  (Figure 10). These findings indicate that asperity effects are more dominant at lower  $D/B$  ratios, whereas at higher ratios the influence of geometry tends to diminish due to the wider distribution of stresses along the contact area.

#### 3.2.2. Evaluation of Theoretical Model Accuracy

The validity of the theoretical predictions is supported by strict control of variables, where the sand material and boundary conditions were kept identical, as well as by the consistency of responses across pile diameters ( $B = 10$ – $15.85$  mm). This is consistent with the design of directional interface tests on snake-scale-inspired surfaces and anisotropic interfaces [43, 44].

Statistical verification was performed using one-way ANOVA, where all comparisons in Table 2 yielded  $p < 0.05$ , while external comparisons in Table 3 reported  $F = 2.305$  with  $p = 0.167$ . This analysis was further validated through the non-parametric Mann–Whitney test, which yielded  $P = 0.166$  ( $P > 0.05$ ). The consistency between parametric and non-parametric outcomes confirms that no significant differences exist between the theoretical results and previous research data, thereby reinforcing the reliability of the quantitative evaluation approach for interface parameters, as commonly adopted in sand–steel friction studies [45].

Moreover, the tendency for capacity to increase at greater depths is consistent—as a mechanistic inference—with findings that anisotropic friction modifies stress distribution and redistribution while enhancing resistance mobilization, even in dilatant sands [43, 46, 47]. Meanwhile, increasingly dominant interlocking has been shown to improve interface shear capacity on rougher surfaces and with more angular particle geometries [45].

#### 3.2.3. Critical Parameters: $C_r$ , Asperities, and Load Transfer Efficiency

The cranial correction factor ( $C_r$ ) is dimensionless and represents the efficiency of end resistance ( $Q_p$ ) enhancement due to the application of cranial asperities at the pile–soil interface. The anisotropic texturing effect, which increases interface shear resistance, has been demonstrated in studies of snake scale-inspired surfaces as well as sawtooth interfaces. A value of  $C_r > 1$  indicates improvement over the Meyerhof baseline under the same soil conditions, whereas  $C_r = 1$  denotes no change.

Asperities are defined by the parameters  $L$  (asperity length) and  $H$  (asperity height), which determine the shape and inclination of the profile and directly influence interface shear behavior. In this study,  $L/H$  ratios of 20, 26.67, and 33.33 were selected as they represent slope variations commonly observed in reptile scale patterns [44] and align with prior recommendations emphasizing the need for geometrical contrasts that remain realistic in terms of manufacturability [43]. Thus, the parameter selection is supported by both biological relevance and existing literature.

Load transfer efficiency is defined as the relative improvement in tip capacity over the Meyerhof baseline under identical soil conditions and boundaries, directly reflected by the  $C_r$  value. The increase in efficiency is consistent with experimental evidence showing that surface texturing patterns significantly enhance the shear strength of sand–steel interfaces.

### 3.2.4. Installation Challenges and Constructability

Micro-texturing on the pile shaft has the potential to increase installation resistance during driving, while simultaneously inducing asperity wear and requiring high geometric precision. To mitigate these adverse effects, the use of wear-resistant materials, chamfering or rounding of asperity tips, modular processing through prefabrication or precision machining, and installation methods that preserve texture integrity are recommended.

Such practices are consistent with the bio-inspired approach, which emphasizes the importance of precision manufacturing in maintaining the functional performance of micro-textures. Similar observations were reported [43], who highlighted that quality control in techniques such as laser texturing and additive manufacturing is a key factor in ensuring the effectiveness of textures in terms of tribological function and mechanical durability [41].

### 3.2.5. Geometric Scale Effects

Within the diameter range of  $B = 10, 12$ , and  $15.85$  mm, the absolute  $Q_p$  value increases with  $B$  ( $Ab \propto B^2$ ), yet the relative efficiency  $C_r$  remains nearly constant across diameters (Figures 8–10). This indicates that geometric ratios such as  $L/H$  are the primary controlling factors. Application of the results to larger diameters requires maintaining relative roughness ( $H/D_{50}, L/D_{50}$ ) to ensure consistency of interaction mechanisms. Recent studies have reported that pile tip resistance in very dense sand increases with diameter, in accordance with the relationship  $Ab \propto B^2$  [48, 49].

Other experimental and numerical findings have shown that particle interlocking significantly influences shear strength and dilation at peak conditions [50]. Moreover, DEM-based simulations indicate that geometric ratios affect overall shear strength and trigger the formation of shear banding, a narrow zone of high strain where granular material failure occurs [51]. Until further verification becomes available, the use of  $C_r$  values is recommended conservatively within the experimental range obtained.

### 3.2.6. Position Within Recent Modifications

Compared to conventional approaches such as helical and under-reamed foundations, which enhance bearing capacity through macro-geometric alterations and installation effects, as well as tapered or cone-top piles that regulate stress distribution by geometric shaping, the snake-skin textured surface proposed in this study offers a distinct working mechanism. This design optimizes pile tip contribution through anisotropic microstructures that are materially efficient and can be readily integrated into the classical Meyerhof bearing capacity formulation via a single modification parameter ( $C_r$ ). Other bio-inspired approaches, such as root-type foundations, have also demonstrated performance gains through different strategies. Branched configurations of root-type piles increased uplift capacity by 30–50% in coral sand [52], while Huang & Martinez [53] showed that root-type anchor systems expanded the active shear zone and significantly enhanced lateral friction mobilization. In contrast, the snake-skin approach emphasizes soil–structure interaction improvement through controlled shear directionality and localized stress mobilization, as described by Martinez & O'hara [12] in their study on selective friction in textured piles. Therefore, this innovation occupies a distinctive position within the current landscape of foundation modifications, combining geometric efficiency, ease of integration into existing models, and biologically inspired surface mechanisms.

### 3.2.7. Practical Design Implications

Optimal performance zone is achieved at a diameter-to-width ratio ( $D/B$ ) of up to 24 (Figures 8–10). Although data are not yet available for ratios above  $D/B > 24$ , there is no evidence of significant structural efficiency gains beyond this range. To ensure both structural and material efficiency, a length-to-height ratio ( $L/H$ ) of 20 is recommended as the most favorable configuration.

Illustrations in Figures 7 and 9 demonstrate that a reduction in element diameter (e.g., from 15.85 mm to 10–12 mm) can be implemented without compromising tip resistance ( $Q_p$ ), provided that the  $D/B$  ratio is maintained. This finding highlights significant opportunities for material savings and carbon footprint reduction. Such outcomes are consistent with the study of Zhang et al. [54], which emphasized the importance of geometric efficiency in sustainable engineering systems.

## 4. Conclusion

This study introduces a modification of Meyerhof's equation by incorporating a cranial correction factor ( $C_r$ ) to account for the influence of the asperity length–height ratio ( $L/H$ ) on the point resistance ( $Q_p$ ) of pile foundations in sandy soils. The analysis shows that an  $L/H$  ratio of 20 represents the most optimal configuration, yielding increases in  $Q_p$  of 11.7–465.8% for a 10 mm diameter pile, 9.7–390.0% for a 12 mm pile, and 7.4–289.7% for a 15.85 mm pile at depths ranging from 10 to 240 mm. The most significant improvements occur at lower  $D/B$  ratios, where stress concentration can be maximized, allowing cranial geometry to partially substitute for larger pile diameters. These findings confirm that more uniform stress distribution and more efficient soil–pile interaction can be achieved through cranial-inspired geometric modifications. Larger  $L/H$  ratios, such as 26.67 and 33.33, still provide capacity improvements, though less effective than  $L/H = 20$ , yet consistently higher than foundations without cranial

modifications. The correction factors obtained— $C_r = 1.07\text{--}5.66$  ( $L/H = 20$ ),  $C_r = 1.07\text{--}4.49$  ( $L/H = 26.67$ ), and  $C_r = 1.07\text{--}3.79$  ( $L/H = 33.33$ )—quantitatively validate the efficiency of this design approach.

Theoretical validation using ANOVA confirmed statistically significant differences ( $p < 0.05$ ) across configurations, while the Mann–Whitney test verified consistency with previous studies. These results indicate that the proposed model reliably describes load transfer in anisotropically textured foundations. From a practical perspective, cranial design offers potential material savings by reducing pile diameters up to 58.5% without compromising tip resistance, thereby improving efficiency and lowering the carbon footprint. However, as this study remains theoretical, further laboratory and field investigations are essential to validate the model and assess its performance under cyclic and long-term loading.

#### 4.1. Limitations and Future Research

The model developed in this study has not yet been verified through field testing, does not account for the variability of soil properties, and does not incorporate material response under cyclic or dynamic loading. Accordingly, future research should include pile load tests in the field with varying  $L/H$  and  $\ell/B$  ratios in asperity configurations to evaluate their contribution to load transfer efficiency, while also examining foundation system performance under diverse geotechnical conditions to assess sensitivity to soil heterogeneity. In addition, the development of nonlinear numerical models capable of realistically representing granular soil behavior is required, along with the evaluation of service life and asperity wear potential to ensure long-term performance sustainability. These recommendations are consistent with the bio-inspired approach, which emphasizes the importance of experimental validation and geometric optimization based on performance outcomes under complex and heterogeneous field conditions.

### 5. Declarations

#### 5.1. Author Contributions

Conceptualization, A.I.C.; methodology, A.I.C.; software, A.I.C.; validation, A.I.C.; formal analysis, A.I.C.; investigation, A.I.C.; resources, A.I.C.; data curation, A.I.C.; writing—original draft preparation, A.I.C.; writing—review and editing, A.M., Y.Z., E.A.S; visualization, A.I.C.; supervision, A.M., Y.Z., E.A.S; project administration, A.I.C.; funding acquisition, A.I.C. All authors have read and agreed to the published version of the manuscript.

#### 5.2. Data Availability Statement

The data presented in this study are available on request from the corresponding author.

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#### 5.4. Conflicts of Interest

The authors declare no conflict of interest.

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